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## GUIDE 98-4

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### Uncertainty of measurement — Part 4: Role of measurement uncertainty in conformity assessment

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## ISO/IEC Foreword

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Draft Guides adopted by the responsible Committee or Group are circulated to the member bodies for voting. Publication as a Guide requires approval by at least 75 % of the member bodies casting a vote.

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ISO/IEC Guide 98-4 was prepared by Working Group 1 of the Joint Committee for Guides in Metrology (as JCGM 106:2012), and was adopted by the national bodies of ISO and IEC.

ISO/IEC Guide 98 consists of the following parts, under the general title *Uncertainty of measurement*:

- *Part 1: Introduction to the expression of uncertainty in measurement*
- *Part 3: Guide to the expression of uncertainty in measurement (GUM:1995)*
- *Part 4: Role of measurement uncertainty in conformity assessment*

The following parts are planned:

- *Part 2: Concepts and basic principles*
- *Part 5: Applications of the least-squares method*

ISO/IEC Guide 98-3 has two supplements:

- *Supplement 1: Propagation of distributions using a Monte Carlo method*
- *Supplement 2: Extension to any number of output quantities*

The following supplement to ISO/IEC Guide 98-3 is planned:

- *Supplement 3: Modelling*

Given that ISO/IEC Guide 98-3:2008/Suppl.1:2011 is identical in content to JCGM 101:2011, the decimal symbol is a point on the line in the English version and a comma on the line in the French version.

Annex ZZ has been appended to provide a list of corresponding ISO/IEC Guides and JCGM guidance documents for which equivalents are not given in the text.

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2012

## Evaluation of measurement data — The role of measurement uncertainty in conformity assessment

Évaluation des données de mesure — Le rôle de l'incertitude de mesure dans l'évaluation de la conformité

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## FOREWORD

In 1997 a Joint Committee for Guides in Metrology (JCGM), chaired by the Director of the Bureau International des Poids et Mesures (BIPM), was created by the seven international organizations that had originally in 1993 prepared the *Guide to the expression of uncertainty in measurement* (GUM) and the *International vocabulary of basic and general terms in metrology* (VIM). The JCGM assumed responsibility for these two documents from the ISO Technical Advisory Group 4 (TAG4).

The Joint Committee is formed by the BIPM with the International Electrotechnical Commission (IEC), the International Federation of Clinical Chemistry and Laboratory Medicine (IFCC), the International Organization for Standardization (ISO), the International Union of Pure and Applied Chemistry (IUPAC), the International Union of Pure and Applied Physics (IUPAP), and the International Organization of Legal Metrology (OIML). A further organization joined these seven international organizations, namely, the International Laboratory Accreditation Cooperation (ILAC).

JCGM has two Working Groups. Working Group 1, "Expression of uncertainty in measurement", has the task to promote the use of the GUM and to prepare Supplements and other documents for its broad application. Working Group 2, "Working Group on International vocabulary of basic and general terms in metrology (VIM)", has the task to revise and promote the use of the VIM. For further information on the activity of the JCGM, see [www.bipm.org](http://www.bipm.org)

Documents such as this one are intended to give added value to the GUM by providing guidance on aspects of the evaluation and use of measurement uncertainty that are not explicitly treated in the GUM. Such guidance will be as consistent as possible with the general probabilistic basis of the GUM.

This document has been prepared by Working Group 1 of the JCGM, and has benefited from detailed reviews undertaken by member organizations of the JCGM and National Metrology Institutes.

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## INTRODUCTION

*Conformity assessment* (see 3.3.1), as broadly defined, is any activity undertaken to determine, directly or indirectly, whether a product, process, system, person or body meets relevant standards and fulfills *specified requirements* (see 3.3.3). ISO/IEC 17000:2004 gives general terms and definitions relating to conformity assessment, including the accreditation of conformity assessment bodies and the use of conformity assessment in facilitating trade.

In a particular kind of conformity assessment, sometimes called *inspection* (see 3.3.2), the determination that a product fulfils a specified requirement relies on measurement as a principal source of information. ISO 10576-1:2003 [22] sets out guidelines for checking conformity with specified limits in the case where a *quantity* (see 3.2.1) is measured and a resulting *coverage interval* (see 3.2.7) (termed ‘uncertainty interval’ in ISO 10576-1:2003) is compared with a *tolerance interval* (see 3.3.5). The present document extends this approach to include explicit consideration of risks, and develops general procedures for deciding conformity based on *measurement results* (see 3.2.5), recognizing the central role of *probability distributions* (see 3.1.1) as expressions of uncertainty and incomplete information.

The evaluation of measurement uncertainty is a technical problem whose solution is addressed by JCGM 100:2008, the *Guide to the expression of uncertainty in measurement* (GUM), and by and its Supplements, JCGM 101:2008, JCGM 102:2011 and JCGM 103 [3]. The present document assumes that a quantity of interest, the *measurand* (see 3.2.4), has been measured, with the result of the measurement expressed in a manner compatible with the principles described in the GUM. In particular, it is assumed that corrections have been applied to account for all recognized significant systematic effects.

In conformity assessment, a measurement result is used to decide if an item of interest conforms to a specified requirement. The item might be, for example, a gauge block or digital voltmeter to be calibrated in compliance with ISO/IEC 17025:2005 [23] or verified according to ISO 3650 [24], or a sample of industrial waste water. The requirement typically takes the form of one or two *tolerance limits* (see 3.3.4) that define an interval of permissible values, called a *tolerance interval* (see 3.3.5), of a measurable property of the item. Examples of such properties include the length of a gauge block, the error of indication of a voltmeter, and the mass concentration of mercury in a sample of waste water. If the true value of the property lies within the tolerance interval, it is said to be conforming, and non-conforming otherwise.

NOTE The term ‘tolerance interval’ as used in conformity assessment has a different meaning from the same term as it is used in statistics.

In general, deciding whether an item conforms will depend on a number of measured properties and there might be one or more tolerance intervals associated with each property. There may also be a number of possible decisions with respect to each property, given the result of a measurement. Having measured a particular quantity, for example, one might decide to (a) accept the item, (b) reject the item, (c) perform another measurement and so on. This document deals with items having a single scalar property with a requirement given by one or two tolerance limits, and a binary outcome in which there are only two possible states of the item, conforming or non-conforming, and two possible corresponding decisions, accept or reject. The concepts presented can be extended to more general decision problems.

In the evaluation of measurement data, knowledge of the possible values of a measurand is, in general, encoded and conveyed by a *probability density function* (see 3.1.3), or a numerical approximation of such a function. Such knowledge is often summarized by giving a best estimate (taken as the *measured quantity value* (see 3.2.6)) together with an associated measurement uncertainty, or a coverage interval that contains the value of the measurand with a stated *coverage probability* (see 3.2.8). An assessment of conformity with specified requirements is thus a matter of probability, based on information available after performing the measurement.

In a typical measurement, the measurand of interest is not itself observable. The length of a steel gauge block, for example, cannot be directly observed, but one could observe the indication of a micrometer with its anvils in contact with the ends of the block. Such an indication conveys information about the length of the block through a measurement model that includes the effects of influence quantities such as thermal expansion and micrometer calibration. In conformity assessment, an accept/reject decision is based on observable data (measured quantity values, for example) that lead to an inference regarding the possible values of a non-observable measurand [37].

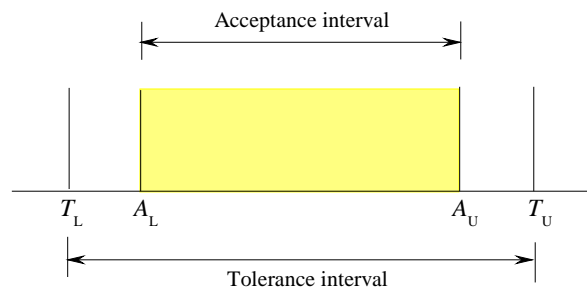
Because of uncertainty in measurement, there is always the risk of incorrectly deciding whether or not an item conforms

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to a specified requirement based on the measured value of a property of the item. Such incorrect decisions are of two types: an item accepted as conforming may actually be non-conforming, and an item rejected as non-conforming may actually be conforming.

By defining an *acceptance interval* (see 3.3.9) of permissible measured values of a measurand, the risks of incorrect accept/reject decisions associated with measurement uncertainty can be balanced in such a way as to minimize the costs associated with such incorrect decisions. This document addresses the technical problem of calculating the *conformance probability* (see 3.3.7) and the probabilities of the two types of incorrect decisions, given a probability density function (PDF) for the measurand, the tolerance limits and the limits of the acceptance interval.

A particular acceptance interval, and its relation to a corresponding tolerance interval is shown in figure 1.



**Figure 1** – Binary conformity assessment where decisions are based on measured quantity values. The true value of a measurable property (the measurand) of an item is specified to lie in a tolerance interval defined by limits ( $T_L, T_U$ ). The item is accepted as conforming if the measured value of the property lies in an interval defined by *acceptance limits* (see 3.3.8) ( $A_L, A_U$ ), and rejected as non-conforming otherwise.

Choosing the tolerance limits and acceptance limits are business or policy decisions that depend upon the consequences associated with deviations from intended product quality. A general treatment of the nature of such decisions is beyond the scope of this document; see, for example, references [14, 15, 34, 35, 36, 44].